

PROBLEMAS DE TRIGONOMETRÍA

Problema 170:

Demostrar que se verifica la igualdad siguiente:

$$\frac{\operatorname{sen} a + \operatorname{sen} b}{\cos a + \cos b} : \frac{\operatorname{sen} a - \operatorname{sen} b}{\cos b - \cos a} = \operatorname{tg}^2 \frac{a+b}{2}$$

Solución Problema 170:

$$\frac{\operatorname{sen} a + \operatorname{sen} b}{\cos a + \cos b} : \frac{\operatorname{sen} a - \operatorname{sen} b}{\cos b - \cos a} = \frac{\operatorname{sen} a + \operatorname{sen} b}{\cos a + \cos b} : \frac{\operatorname{sen} a - \operatorname{sen} b}{-(\cos b - \cos a)} = \frac{\operatorname{sen} a + \operatorname{sen} b}{\cos a + \cos b} : \frac{\operatorname{sen} a - \operatorname{sen} b}{-(\cos a - \cos b)}$$

$$\frac{2\operatorname{sen} \frac{a+b}{2} \cdot \cos \frac{a-b}{2}}{2\cos \frac{a+b}{2} \cdot \cos \frac{a-b}{2}} : \frac{2\cos \frac{a+b}{2} \cdot \operatorname{sen} \frac{a-b}{2}}{-[-2\operatorname{sen} \frac{a+b}{2} \cdot \operatorname{sen} \frac{a-b}{2}]} = \frac{\operatorname{sen} \frac{a+b}{2}}{\cos \frac{a+b}{2}} : \frac{\cos \frac{a+b}{2}}{\operatorname{sen} \frac{a+b}{2}} = \operatorname{tg} \frac{a+b}{2} : \operatorname{cotg} \frac{a+b}{2} =$$

$$\operatorname{tg} \frac{a+b}{2} : \frac{1}{\operatorname{tg} \frac{a+b}{2}} = \operatorname{tg}^2 \frac{a+b}{2}$$